## St. Mary's Catholic Primary School



How we teach calculations:

### Calculation Policy for Mathematics

March 2014

# Albout our Calculation Policy

smooth progression of learning in calculations across the school. Please note that early learning in num-Years Foundation Stage policy is designed to build on progressively from the content and methods established in the Early ber and calculation in Reception follows the 'Development Matters' EYFS document, and this calculation for thé teaching and learning of mathematics, and is also designed to give pupils a cohsistent and The following calculation policy has been devised to meet requirements of the National Curriculum 2014

### Age stage expectations

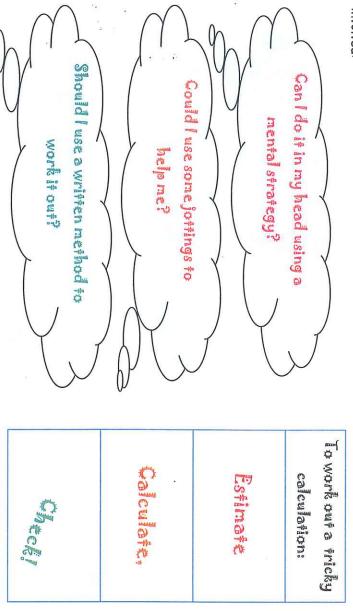
stage until they are secure enough to move on currently working at, being moved onto the next level as soon as they are ready, or working at a lower Curriculum 2014, however it is vital that pupils are taught according to the stage that they are The calculation policy is organised according to age stage expectations as set out in the National

## Providing a context for calculation:

calculation lessons. use certain operations and methods when faced with problems. This must be a priority within help build children's understanding of the purpose of calculation, and to help them recognise when to It is important that any type of calculation is given a real life context or problem solving approach to

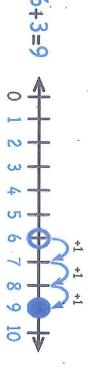
## Choosing a calculation method:

involved: they will take to a calculation, to ensure they select the most appropriate method for the numbers Children need to be taught and encouraged to use the following processes in deciding what approach



## Year 1 Add with numbers up to 20

to start with the larger number and count on Use numbered number lines to add, by counting on in ones. Encourage children



#### Children should:

contexts. horizontal, vertical, circular etc.) and be shown numbers in different number tracks and number lines (ensure number lines are varied e.g. Have access to a wide range of counting equipment, everyday objects,

If possible, use two different colours of base 10 equipment so that the initial amounts can still be seen.

11+5=

11+	,	<b>F</b>	
5 = 16		N	
6	*	ω	
		4	
		OI	
		0,	
		7	
		œ	
		v	
		10	
		E	
A		12	
	le l	13	
_ [		14	
		51	
		16	
	F-1-	17	
		18	

tences. Read and write the addition (+) and equals (=) signs within number sen-

Model of Base 10 equipment

using concrete objects and number line addition to solve them:  $8 \div 3 = \Box$ Interpret addition number sentences and solve missing box problems, 15 + 4 = 5 + 3 + 1 = □ + □ = 6

into one group (5 cubes and 3 cubes) in Early Years This builds on from prior learning of adding by combining two sets of objects

Bead strings or bead bars can be used to illustrate addition including bridging through ten by counting on 2 then counting on 3.

**©**9



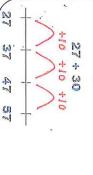
Key skills for addition at Y1:

- Read and write numbers to 100 in numerals, incl. 1—20 in words
- Recall bonds to 10 and 20, and addition facts within 20
- Count to and across 100
- Count in multiples of 12,5 and 10
- Solve simple 1-step problems involving addition, using objects, number lines and pictorial

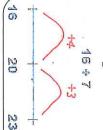
#### Year Add with 2-digit numbers Developing mental fluency with

addition and place value involving 2-digit numbers, then establish more formal methods

Add 2-digit numbers and tens:



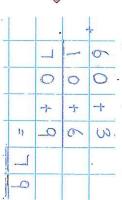
#### Add 2-digit numbers and units:



mental addition skills confidence and fluency in squares etc. to build concrete equipment, hundred Use empty number lines,

Add pairs of 2-digit numbers, moving to the partitioned column method when





are secure with the examples that do NOT cross the tens STEP 1:Only provide boundary until they

They will record

for the 10 rods

method itself.

Children will continue to use the Base 10 equipment to support their calculations, the calculations using their own drawings of the Base 10 equipment (as lines for t dots for the unit blocks)

e.g. 34 + 23 =

6

73

S 1

They would add the units first and then the tens before combining them.

00

UT N W 0 0 0

number mentally (e.g. 80+11), they 2-digit numbers that DO cross are ready for adding pairs of multiple of ten to a 2-digit STEP 2: Once children can add

the tens boundary (e.g.  $58 \div 43$ )

\_0 50 0 0 + 43: 00 (v) 0

numbers (see Y3) the expanded addition this stage should move onto methods with 2 and 3-digit confident and accurate with STEP 3: Children who are

28 + 36 = 64

When the units total more than 10, children should be encouraged to exchange 10 units for 1 ten. This is the start of children understandina 'carryina' in vertical addition.

SUN 0 + F

0

0

Key vocabulary: count on; number line, sum, add, more, tens, plus, units, partition, addition, column, tens boundary and, make, altogether, total, equal to, equals, double, most,

### Key skills for addition at Y2:

- Add a 2-digit number and ones (e.g.  $27 \div 6$ )
- Add a 2-digit number and tens (e.g.  $23 \div 40$ )
- Add pairs of 2-digit numbers (e.g.  $35 \div 47$ )
- Add three single-digit numbers (e.g. 5 + 9 + 7)
- Show that adding can be done in any order (the commutative law).
- 0 Recall bonds to 20 and bonds of tens to 100 (30 + 70 etc.)
- 0 0 Count in steps of 2, 3 and 5 and count in tens from any number Understand the place value of 2-digit numbers (tens and ones)
- Compare and order numbers to 100 using < > and = signs.

0

- Read and write numbers to at least 100 in numerals and words
- Solve problems with addition, using concrete objects, pictorial representations, involving numbers

#### Addition

## Year 3 Add numbers with up to 3-digits

Introduce the expanded column addition method:

32-700-900-93

Add the units first, in preparation for the compact method.

In order to carry out this method of addition:

- Children need to recognise the value of the hundreds, tens and units without recording the partitioning.
- Pupils need to be able to add in columns.

Move to the compact column addition method, with 'carrying':

Add units first.

Add units first.

+ 73

'Carry' numbers
underneath the
bottom line.

1

Children who are very secure and confident with 3-digit expanded column addition should be moved onto the compact column addition method, being introduced to 'carrying' for the first time. Compare the expanded method to the compact column method to develop an understanding of the process and the reduced number of steps involved.

Remind pupils the actual value is 'three tens add seven tens', not 'three add seven', which equals ten tens.

number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, increase, vertical, 'carry', expanded, compact

### Key skills for addition at V3:

- Read and write numbers to 1000 in numerals and words.
- Add 2-digit numbers mentally, incl. those exceeding 100.
- Add a three-digit number and ones mentally (175 + 8)
- Add a three-digit number and tens mentally (249 + 50)
- Add a three-digit number and hundreds mentally (381 + 400)
- Estimate answers to calculations, using inverse to check answers
- Solve problems, including missing number problems, using
- number facts, place value, and more complex addition.
- Recognise place value of each digit in 3-digit numbers (hundreds, tens, ones.)
- multiple of 10, 100, 100 and adjusting, using near doubles, partitioning and recombining Continue to practise a wide range of mental addition strategies, ie. number bonds, adding the nearest

### Year 4 Add numbers with up to 4 digits



measures contexts. first, and 'carrying' numbers underneath the calculation. Also include money and Move from expanded addition to the compact column method, adding units

Add units first.

with (expanded column addition—see Y3). Teacher models the compact method with carrying, asking gether using the method that they are familiar children to discuss similarities and differences and asking children to add the two given numbers toestablish how it is carried out. Introduce the compact column addition method by

them the actual value is 5 hundreds add 3 hundreds, not 5 Reinforce correct place value by reminding add 3, for example.

Use and apply this method to money and measurement values

cross them off bottom line and underneath the Carry numbers

counted

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on increase, vertical, 'carry', expanded, compact, thousands, hundreds, number line, sum, tens, units, partition, plus, addition, column, tens boundary, digits, inverse hundreds boundary,

### Key skills for addition at Y4:

- Select most appropriate method: mental, jottings or written and explain why.
- Recognise the place value of each digit in a four-digit number.
- Round any number to the nearest 10, 100 or 1000
- Estimate and use inverse operations to check answers
- Solve 2-step problems in context, deciding which operations and methods to use and why.
- Find 1000 more or less than a given number.
- nearest multiple of 10, 100, 1000 and adjust, use near doubles, partitioning and recombining Continue to practise a wide range of mental addition strategies, ie. number bonds, add the
- Add numbers with up to 4 digits using the formal written method of column addition
- Solve 2-step problems in contexts, deciding which operations and methods to use and why
- Estimate and use inverse operations to check answers to a calculation.



places.

### year 5 Add numbers with more than 4

including money, measures and decimals with different numbers of decimal

way as the other place value columns, and must be in the same column in the answer. The decimal point should be aligned in the same

Numbers should exceed 4 digits

carefully aligning place value columns. Pupils should be able to add more than two values

Empty decimal places can be filled with zero to show the place value in each column

Children should:

to reinforce place value Say '6 tenths add 7 tenths'

align numbers with different numbers of decimal places Understand the place value of tenths and hundredths and use this to

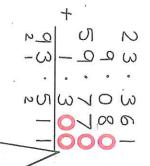
Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, decimal point, tenths, hundredths, thousandths increase, 'carry', expanded, compact, vertical, thousands, hundreds, digits, inverse & decimal places number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary,

### Key skills for addition at Y5:

- ie. add the nearest multiple of 10, 100, 100 and adjust; use near doubles, inverse, partitioning and re-combining; using number bonds. Add numbers mentally with increasingly large numbers, using and practising a range of mental strategies
- Use rounding to check answers and accuracy.
- 0 Solve multi-step problems in contexts, deciding which operations and methods to use and why
- . Read, write, order and compare numbers to at least 1 million and determine the value of each digit
- . Round any number up to 1 000 000 to the nearest 10, 100, 1000, 10 000 and 100 000.
- Add numbers with more than 4 digits using formal written method of columnar addition.



# Add several numbers of increasing complexity



Adding several numbers with different numbers of decimal places (including money and measures):

- Tenths, hundredths and thousandths should be correctly aligned, with the decimal point lined up vertically including in the answer row
- Zeros could be added into any empty decimal places, to show there is no value to add.

Empty decimal places can be filled with zero to show the place value in each column.

Adding several numbers with more than 4 digits.

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, point, tenths, hundredths, thousandths increase, 'carry', expanded, compact, vertical, thousands, hundreds, digits, inverse, decimal places, decima number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, most, count on,

### Key skills for addition at Y6:

- practising a range of mental strategies. Perform mental calculations, including with mixed operations and large numbers, using and
- Solve multi-step problems in context, deciding which operations and methods to use and why.
- Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy.
- Read, write, order and compare numbers up to 10 million and determine the value of each digit.
- Round any whole number to a required degree of accuracy.
- complexity. Pupils understand how to add mentally with larger numbers and calculations of increasing

Solve one-step problems that involve addition and subtraction, using concrete objects (ie bead string

and mintimos and mission number machlems

7410.47

#### ear 2 Subtract with 2-digit numbers

mental subtraction skills Subtract on a number line by counting back, aiming to develop

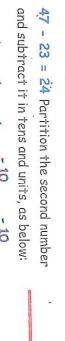
Use Dienes blocks calculations too for subtraction

This strategy will be used for:

- 2-digit numbers subtract units (by taking away / counting back) e.g., 36
- 2-digit numbers subtract tens (by taking away / counting back) e.g. 48—30
- Subtracting pairs of 2-digit numbers (see below:)

#### Subtracting pairs 0 <del>1</del> 2-digit numbers 000 a number line:

47 - 23 = 24 Partition the second number





L

Subtract tens

first.

24

jumps back, as below: Move towards more efficient 20

24 27

Combine methods with use of a hundred square to reinforce understanding of number value and order.

N

Then subtract units.

can help them to become more efficient, for Teaching children to bridge through ten

example 42—25:

Use Sienes blocks.

for subpaction

calculations too.

17 20

22

Children will move on to using the Base 10 equipment to support their calculations. They need to understand that the number being subtracted does not appear as an amount on iown, but rather as part of the larger amount.

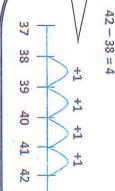
e.q. 39-17=

on its The Sunich Course Support of the suppor 20 String Whith Who will have been a second

Children would count out 39 using the Base 10 equipment (3 tens and 9 units) and would remove 7 units and then one ten, counting up the answer of 2 tens and 2 units to give 22.

Mental strategy - subtract numbers close together by counting on:

and count on to smaller number Start with the the largest



about the relationship between addition and subtraction Many mental strategies are taught. Children are taught to efficient to count on the difference. They need to be clear recognise that when numbers are close together, it is more

difference, many more, Key vocabulary: equal to, take, how many fewer / less than, most, least, count back , how many left, how much less is count on, strategy, partition, tens, take away, less, minus, subtract, leaves, distance between, units how

#### Ke V skills for subtraction at y2:

- Recognise the place value of each digit in a two-digit number.
- Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100
- digit number and ones, a two-digit number and tens, and two two-digit numbers Subtract using concrete objects, pictorial representations, 100 squares and mentally, including: a two-
- 0 Show that subtraction of one number from another cannot be done in any order
- tions and missing number problems. Recognise and use inverse relationship between addition and subtraction, using this to check calcula-
- representation, and also applying their increasing knowledge of mental and written methods Solve simple addition and subtraction problems including measures, using concrete objects, pictoria
- Dond and write numbers to at least 100 in numerals and in wards

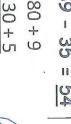
### COT Subtracting with 2 and 3-digit numbers

Introduce partitioned column subtraction method

exchanging is examples where no this method with STEP 1: introduce

required.

50+





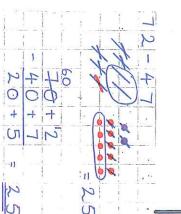




equipment is used so that It is essential that Base 10 subtraction is carried out practically.

### 2: Introduce 'exchanging' through practical subtraction

- 1) Make the larger number (72) with Base 10.
- Subtract 47, starting with the units.
   Children should recognise that there are not enough units to take 7 away.
- 4) They exchange one ten for ten units (to be carried out in red so the children can see this step clearly).
- 5) Children now take away 7.units, crossing them out as they 90
- Then take away 4 tens.
- 7) Circle the remaining tens and units to find the answer.



with the understanding of STEP 3: Once pupils are secure

subtract any 2 and 3-digit numbers partitioned column method to 'exchanging', they can use the

	'			1 1
-	_	N	_	N
	0	ø	0	w
0	0	6	0	00
+	+	+		1
_0	4	W		-
0	0	0		F
+	+	+		0
10	9	00		11
				0
				10

#### £1+30p+8p Subtracting money: partition into e.g.

## Counting on as a mental strategy for subtraction

add tens first then units (link to

Show the children both methods:

- number bond to multiples of 10/100/1000 on each jump until

Children to decide which method they are most comfortable with.

Continue to reinforce counting on as a strategy for close-together numbers (e.g. 121—118), to count on (e.g. 102-89, 131-79, or calculating change from £1 etc.) and also for numbers that are 'nearly' multiples of 10, 100, 1000 or £s, which make it easier



on, strategy, partition, tens, units exchange, how many fewer / less than, most, least, count back , how many left, how much less is\_? difference, Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, decrease, hundreds, value, digit

### Key skills for subtraction at Y3:

- Subtract mentally a: 3-digit number and ones, 3-digit number and tens, 3-digit number and hundreds
- Estimate answers and use inverse operations to check.
- Solve problems, including missing number problems.
- Find 10 or 100 more or less than a given number.
- Recognise the place value of each digit in a 3-digit number .
- Counting up differences as a mental strategy when numbers are close together or near multiples of 10 (see examples above)
- Read and write numbers up to 1000 in numerals and words.

o o

Practise mental subtraction strategies, such as subtracting near multiples of 10 and adjusting (e.g. subtracting 19 or 21), and select most appropriate methods to subtract, explaining why.



## ear 4 Subtract with up to 4-digit numbers

Partitioned column subtraction with 'exchanging' (decomposition):

Compact column subtraction (see video)

and values. Use place value countowards more complex numbers ters to reinforce 'exchanging' As introduced in Y3, but moving

into £1 + 30 + 5 for example. Subtracting money: partition

apply this to money and measures. Give plenty of opportunities to

> to perform a subtraction calculation with the and what is different, to develop an they have done. Ask pupils to consider how it display the compact version for the calculation familiar partitioned column subtraction then understanding of it (shown on video). relates to the method they know, what is similar To introduce the compact method, ask children

ten method mental, counting on, counting back or writbest method for the numbers involved-Always encourage children to consider the

#### Mental strategies

A variety of mental strategies must be taught and practised, including counting on to find the difference where numbers are closer together, or where it is easier to

Calculate, Check!

Estimate

count on (see video below).

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, distance be-

less is\_? difference, count on, strategy, partition, tens, units exchange, decrease, hundreds, value, digit, tween, how many more, how many fewer / less than, most, least, count back , how many left, how much

### Key skills for subtraction at Y4:

- Subtract by counting on where numbers are close together or they are near to multiples of 10, 100 etc.
- Children select the most appropriate and efficient methods for given subtraction calculations
- Estimate and use inverse operations to check answers.
- Solve addition and subtraction 2-step problems, choosing which operations and methods to use and why
- Solve simple measure and money problems involving fractions and decimals to two decimal places
- Find 1000 more or less than a given number.
- Count backwards through zero, including negative numbers.
- Recognise place value of each digit in a 4-digit number Round any number to the nearest 10, 100 or 1000
- Solve number and practical problems that involve the above, with increasingly large positive numbers.

## 5 Subtract with at least 4-digit numbers

including money, measures, decimals

(with 'exchanging'). Compact column subtraction

column method until ready remain on the partitioned and place value will need to secure with number facts for the compact method. Children who are still not

Subtracting with larger integers

of integers and decimals, aligning the decimal Subtract with decimal values, including mixtures

with money and measures. subtracting and finding differences Create lots of opportunities for

> what to subtract in that column. places to aid understanding of Add a 'zero' in any empty decima

Key vocabulary: equal to, exchange, decrease, hundreds, value, digit, inverse, tenths, hundredths, decimal point, decima many left, how much less is\_? difference, count on, strategy, partition, tens, units between, how many more, how many fewer / less than, most, least, count back , how take, take away, less, minus, subtract, leaves, distance

Calculate,

Check!

Estimate,

### Key skills for subtraction at Y5:

- Subtract numbers mentally with increasingly large numbers.
- Use rounding and estimation to check answers to calculations and determine, in a range of contexts, levels of accuracy.
- Solve addition and subtraction multi-step problems in context, deciding which operations and methods to use and why.
- Read, write, order and compare numbers to at least 1 million and determine the value of each digit
- Count forwards or backwards in steps of powers of 10 for any given number up to 1 million.
- Interpret negative numbers in context, counting forwards and backwards with positive and negative integers through 0.
- Round any number up to 1 million to the nearest 10, 100, 1000, 10000 and 100000

#### Year Subtracting with increasingly large and more complex numbers and decimal values

Using the compact column method to subtract more complex integers

Using the compact column method to subtract money and measures, including decimals with different numbers of decimal places.

Empty decimal places can be filled with zero to show the place value in each column.

mental recall skills, and informal and formal written methods when selecting the Pupils should be able to apply their knowledge of a range of mental strategies most appropriate method to work out subtraction problems

If the numbers involved in the calculation are close together or near to multiples of 10, 100 gtc, children should be encouraged to recognise that it is more efficient to find the difference by counting up using a number line to support the mental calculation. e.g. 3002 - 1997 = 1005

+3 +2 +2 1997 2000 3000 3002

Key vocabulary: decrease, hundreds, value, digit, inverse, tenths, hundredths, decimal point, decimal back , how many left, how much less is\_? difference, count on, strategy, partition, tens, units tance between, how many more, how many fewer / less than, most, least, count equal to, take, take away, less, minus, subtract, leaves, dis-Check!

exchange,

Estimate,

### Key skills for subtraction at Y6:

- to use and why. Solve addition and subtraction multi-step problems in context, deciding which operations and methods
- Read, write, order and compare numbers up to 10 million and determine the value of each digit
- Round any whole number to a required degree of accuracy
- Use negative numbers in context, and calculate intervals
- o : across zero.
- Children need to utilise and consider a range of mental subtraction strategies, jottings and written methods before choosing how to calculate

Soo previous videos for introducing the compact column method

#### tiplication

### pictorial representations. Multiply with concrete objects, arrays and

-How many legs will 3 teddies have?



There are 3 sweets in one bag. How many sweets are in 5 bags altogether?











- 5s and 10s Give children experience of counting equal group of objects in 2s,
- Present practical problem solving activities involving counting equal sets or groups, as above

wrapping paper etcand use this in their learning answering questions such as 'How many Children will use practical equipment to make groups of objects to represent multiplication eggs would we need to fill the egg box? How do you know? They should see everyday versions of arrays, e.g. egg boxes, baking trays, ice cube trays

Key vocabulary: groups of, lots of, times, array, altogether, multiply, count

Key skills for multiplication at Y1:

Count in multiples of 2, 5 and 10.

pictorial representations and arrays with the support of the teacher Solve one-step problems involving multiplication, by calculating the answer using concrete objects,

Make connections between arrays, number patterns, and counting in twos, fives and tens

Begin to understand doubling using concrete objects and pictorial representations

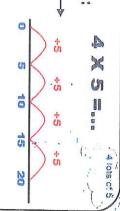
### Year Multiply using arrays and repeated addition



(using at least 2s, 5s and 10s)

#### Cse repeated addition on a number line:

write multiplication statements using x and = signs a number line to work out multiplication facts and Starting from zero, make equal jumps up on



OSO OSO arrays:

W

×

UI

CI

+

OI

4

S

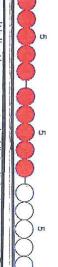
11

5

multiplication, and give examples such as 3  $\times$ Use arrays to help teach children to understand the commutative law of II

5 x 3 = 5 + 5 +

Use practical apparatus:



Childrenshould continue to utilise multiplication as repthis knowledge will support with the development of to support their calculation. These should be supporte paper, e.g. f the grid meth edby the use of

x	x	x	x
х	х	х	х
х	х	x	х
х	х	x	х
x	х	x	.χ
х	х	x	χ
x	х	×	х

7+7+7+7=

(For mathematical accuracy the above example is actually 7 x 4 i.e. Seven, four times, however, because we use terms such as 'groups of' or 'lots of', children are more familian with the initial notation. Once children understand the commutative order of multiplication the order is irrelevant).

#### Use mental recall:

through practice in counting and understanding of the operation Children should begin to recall multiplication facts for ÍN OI and 10 times tables

addition, column, Key vocabulary: row, groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated commutative, sets of, equal groups, times as big as, once, twice, three times.

#### Key skills for multiplication at Y2:

- Count in steps of 2, 3 and 5 from zero, and in 10s from any number
- and evens Recall and use multiplication facts from the 2, UI and 10 multiplication tables, including recognising odds
- Write and calculate number statements using the x and =
- Show that multiplication can be done in any order (commutative).
- mental methods, and multiplication facts Solve a range of problems involving multiplication, using concrete objects, arrays, repeated addition,
- Pubils use a variety of language to discuss and describe multiplication

Multiplication

#### year Multiply 2-digits by a single digit number

Introduce the grid method for multiplying 2-digit by single-digits:

Link the layout of the grid to an array initially:

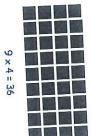
Eg. 23 x 8 = 184

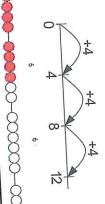
00	×
160	20
24	co

Introduce the grid method with children physically making an array to represent the this to grid method format (see video clip). calculation (e.g. make 8 lots of 23 with 10s and 1s place value counters), then translate

#### 7 do this, children must be able

- Partition numbers into tens and units
- Multiply multiples of ten by a single digit (e.g.  $20 \times 4$ ) using their knowledge of multiplication facts and place value 3, 4, 5, 8 and 10 times tables
- Recall and work out multiplication facts in the 2, Work out multiplication facts not known by repeated addition or other taught
- mental strategies (e.g. by commutative law, working out near multiples and adjustnumber line, bead bars and arrays: ing, using doubling etc.) Strategies to support this are repeated addition using a





Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated ad-

dition, column, row, commutative, sets of, equal groups, times, partition, grid method, multiple, product, tens, units, value

- Xey skills for multiplication: Recall and use multiplication facts for the 2, 3, 4, 5, 8 and 10 multiplication tables, and multiply
- Write and calculate number statements using the multiplication tables they know, including 2-digit imes
- single-digit, drawing upon mental methods, and progressing to reliable written methods Solve multiplication problems, including missing number problems.
- Develop mental strategies using commutativity (e.g.  $4 \times 12 \times 5 = 4 \times 5 \times 12 = 20 \times 12 = 240$ )
- Solve simple problems in contexts, deciding which operations and methods to use.
- Develop efficient mental methods to solve a range of problems e.g using commutativity (4 imes 12 imes
- 4 × 5 × 12 =  $20 \times 12 = 240$ ) and for missing number problems

Multiplication

### Multiply 2 and 3-digits by a single digit, using

all multiplication tables up to 12 imes 12

Developing the grid method:

150 500 30 addition to add Encourage column accurately

680

and accurate multiplying 2 and 3-digit numbers by a single digit this way, and Move onto short multiplication (see Y5) if and when children are confident are already confident in 'carrying' for written addition

### Children should be able to:

calculating, going back to the approximation to check the reasonableness of their answer. e.g: Approximate before they calculate, and make this a regular part of their

"346  $\times$  9 is approximately 350  $\times$  10 = 3500"

Record an approximation to check the final answer against

Multiply multiples of ten and one hundred by a single-digit, using their multiplication table knowledge.

> Estimate,, Calculate, Check!

Recall all times tables up to  $12 \times 12$ 

Key vocabulary: addition, array, column, row, commutative, groups of, sets of, lots of, equal groups, times, multiply, times as big as, once, twice, three times... partition, grid method, total, multiple, product, sets of, inverse groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated

### Key skills for multiplication at Y4:

- Count in multiples of 6, 7, 9, 25 and 1000
- Recall multiplication facts for all multiplication tables up to 12 imes 12
- Use place value, known facts and derived facts to multiply mentally, e.g. multiply by 1, 10, 100, by 0, or to Recognise place value of digits in up to 4-digit numbers
- multiply 3 numbers. Use commutativity and other strategies mentally  $3 \times 6 = 6 \times 3$ ,  $2 \times 6 \times 5 = 10 \times 6$ ,  $39 \times 7 = 30 \times 7 + 9 \times 7$ .
- Solve problems with increasingly complex multiplication in a range of contexts

0

- Recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) Count in multiples of 6, 7, 9, 25 and 1000

#### iplication

#### Year Multiply up to 4-digits by <u>\_</u> 07 2 digits



Introducing column multiplication

- in the column method (see video). od, to see how the steps are related, but notice how there are less steps involved Introduce by comparing a grid method calculation to a short multiplication meth-
- Children need to be taught to approximate first, e.g. for 72 imes 38, they will use rounding: to check the reasonableness of their answer against  $72 \times 38$  is approximately  $70 \times 40 = 2800$ , and use the approximation

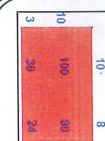
## Short multiplication for multiplying by a single digit

4	×
1200	300
80	20
28	7



Pupils could be asked to work out a given calculation using the grid, and then compare it to 'your' column method. What are the similarities and differences? Unpick the steps and show how it reduces the steps.

#### Introduce long multiplication for multiplying by N digits, using the grid first







18  $\times$  3 on the 1st row (8  $\times$  3 = 24, carrying the 2 for twenty, then '1'  $\times$  3).

 $\frac{18 \times 10}{2}$  on the 2nd row. Put a zero in units first, then say  $8 \times 1$ , and  $1 \times 1$ .

Moving towards more complex numbers

The grid could be used to introduce long multiplication, as the relationship can be seen in the answers in each row.

Calculate,
Check!

dition, column, row, commutative, sets of, equal groups, \_times as big as, once, Key vocabulary groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated adplication, tion, grid method, total, multiple, product, inverse, square, factor, integer, decimal, short/long multi-COMMY twice, three times..., parti-

### Key skills for multiplication at Y5:

Identify multiples and factors, using knowledge of multiplication tables to 12×12

Solve problems where larger numbers are decomposed into their factors

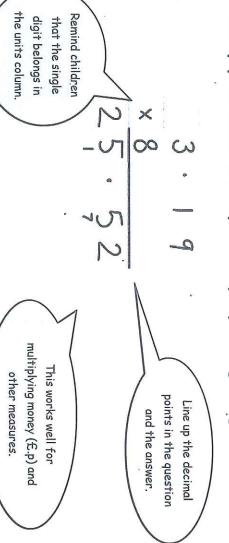
Multiply and divide integers and decimals by 10, 100 and 1000

Recognise and use square and cube numbers and their notation

Solve problems involving combinations of operations, choosing and using calculations and methods appropriately.

#### tiplication

multiply decimals with up to 2d.p by a single digit. Short and long multiplication as in Y5, and



Children will be able to:

- these to check answers against. Use rounding and place value to make approximations before calculating and use
- up to 2d.p. by a single digit. by a single digit; to multiply money and measures, and to multiply decimals with Use short multiplication (see Y5) to multiply numbers with more than 4-digits
- Use long multiplication (see Y5) to multiply numbers with at least 4 digits by a 2-digit number.

Estimate,
Calculate,
Check!

partition, grid method, total, multiple, product, inverse, square, factor, integer, decimal, short / long muldition, array, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times... Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated adtiplication, 'carry', tenths, hundredths, decimal

Key skills for multiplication at Y6:

- Recall multiplication facts for all times tables up to  $12 \times 12$  (as Y4 and Y5)
- Multiply multi-digit numbers, up to 4-digit  $\times$  2-digit using long multiplication.
- Perform mental calculations with mixed operations and large numbers
- tions and methods. Solve multi-step problems in a range of contexts, choosing appropriate combinations of opera-
- Estimate answers using round and approximation and determine levels of accuracy
- Round any integer to a required degree of accuracy.



## Year 1 Group and share small quantities

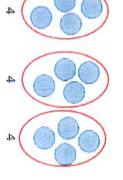
ing both grouping and sharing Using objects, diagrams and pictorial representations to solve problems involv-

How many groups of 4 can be made with 12 stars? = 3

Grouping:



Sharing:



12 shared between 3 is 4

Example division problem in a familiar context:

There are 6 pupils on this table and there are 18 pieces of fruit to share between us. If we share them equally, how many will we each get?

Can they work it out and give a division statement...?

"18 shared between 6 people gives you 3 each."

#### Pupils should :

- use lots of practical apparatus, arrays and picture representations
- between 2 people) Be taught to understand the difference between 'grouping' objects (How many groups of 2 can you make?) and 'sharing' (Share these sweets
- Be able to count in multiples of 2s, 5s and 10s.
- Find half of a group of objects by sharing into 2 equal groups

Key Vocabulary: share, share equally, one each, two each..., group, groups of, lots of, array

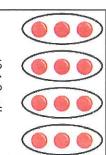
## Key number skills needed for division at Y1:

- concrete objects, pictorial representations arrays with the support of the teacher Solve one-step problems involving multiplication and division, by calculating the answer using
- simple fractions of objects, numbers and quantities. Through grouping and sharing small quantities, pupils begin to understand, division, and finding
- They make connections between arrays, number patterns, and counting in twos, fives and tens





grouping on a number line.



This represents  $12 \div 3$ , posed as how many groups of 3 are in 12?

Pupils should also show that the same array can represent 12 ÷ 4 = 3 if grouped horizontally.

## 

## Know and understand sharing and grouping:

6 sweets shared between 2 people, how many do they each get?

hey each get?

Grouping

Grouping

Grouping

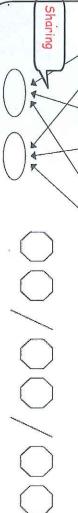
Grouping

Grouping

Grouping

Grouping

Grouping

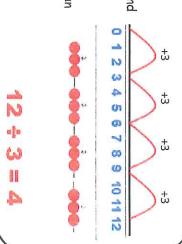


Children should be taught to recognise whether problems require sharing or grouping

### Grouping using a number line:

Group from zero in equal jumps of the divisor to find out 'how many groups of \_ in \_ ?'. Pupils could and using a bead string or practical apparatus to work out problems like 'A CD costs £3. How many CDs can I buy with £12?' This is an important method to

I buy with £12?' This is an important method to develop understanding of division as grouping.



Pose 12 ÷ 3 as 'How many groups of 3 are in 12?'

Key Vocabulary: share, array, divide, divided by, divided into, share equally, one each, division, grouping, number two each... group, line, equal groups of, left over lots 30

## Key number skills needed for division at Y2:

- Count in steps of 2, 3, and 5 from 0
- Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers.
- Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the x, + and = signs
- Show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot.
- methods, and multiplication and division facts, including problems in contexts Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental

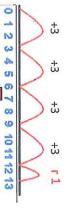


### (where there is no remainder in the final answer) Year 3 Divide 2-digit numbers by a single digit



Grouping on a number line: 4 7 <u>\_\_\_</u>

<u>ر</u> را،



remainders across within the short division method being translated to a number line. Children should work should be introduced practically and with arrays, as well as facts by grouping on a number line from zero. mentally for the 2s, 3s, 4s, 5s, 8s and 10s, ready for 'carrying towards calculating some basic division facts with remainders now taught the concept of remainders, as in the example. This STEP 1: Children continue to work out unknown division They are also

(each digit must be a multiple of the divisor). Short division: Limit numbers to NO remainders in the answer OR carried

used

need to be contexts Real life

is equal to 90 and 6, but in short division, pose: Remind children of correct place value, that 96 carefully selected examples requiring no calculating of

remainders at all. Start by introducing the layout of short

division by comparing it to an array.

5.6

for larger 2-digit numbers should be introduced, initially with

demonstrate this using number lines, arrays etc., short division STEP 2: Once children are secure with division as grouping and

- How many 3's in 9? = 3, and record it above the 9 tens.
- How many 3's in 6? = 2, and record it above the 6 units.

with remainders occurring within the NO remainders in the final answer, but Short division: Limit numbers to

recognise ability to ing, and the understandgain a full help pupils routinely to



problems

how to apply division and the place of

the number line to work out individual division facts that remainder onto the next digit. If needed, children should use within the calculation (e.g. 96÷4), and be taught to 'carry' the can be taught how to use the method when remainders occur remainders, and also the short division method taught, they STEP 3: Once children demonstrate a full understanding of occur which they are not yet able to recall mentally.

Step 3 Only taught when pupils can calculate 'remainders'

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, remainder, multiple short division,

## Key number skills needed for division at Y3:

- bling, connect the 2, 4 and 8s). Recall and use multiplication and division facts for the 2, 3, 4, 5, 8 and 10 multiplication tables (through dou-
- that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to for-Write and calculate mathematical statements for multiplication and division using the multiplication tables mal written methods.
- Solve problems, in contexts, and including missing number problems, involving multiplication and division
- 0 6,  $6 \div 3 = 2$  and  $2 = 6 \div 3$ ) to derive related facts  $(30 \times 2 = 60, \text{ so } 60 \div 3 = 20 \text{ and } 20 = 60 \div 3)$ . Pupils develop efficient mental methods, for example, using multiplication and division facts (e.g. using  $3 \times 2$
- Pupils develop reliable written methods for division, starting with calculations of 2-digit numbers by 1-digit numbers and progressing to the formal written method of short division.



### year 4 Divide up to 3-digit numbers by a single

(without remainders initially)

Continue to develop short division:

Short division should only be taught once children have secured the skill of calculating 'remainders'.



STEP 1: Pupils must be secure with the process of short division for dividing 2-digit numbers by a single digit (those that do not result in a final remainder—see steps in Y3), but must understand how to calculate remainders, using this to 'carry' remainders within the calculation process (see example).

need to be

contexts

Real life

gain a full

routinely to help pupils

understanding, and the ability to

recognise

STEP 2: Pupils move onto dividing numbers with up to 3-digits by a single digit, however problems and calculations provided should not result in a final answer with remainder at this stage. Children who exceed this expectation may progress to Y5 level.



problems.

how to apply

the place of division and

When the answer for the first column is zero  $(1 \div 5$ , as in example), children could initially write a zero above to acknowledge its place, and must always 'carry' the number (1) over to the next digit as a remainder.

Include money and measure contexts when confident.

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry' remainder, multiple, divisible by, factor

Key number skills needed for division at Y4:

- Recall multiplication and division facts for all numbers up to 12 imes 12
- dividing by 10 and 100 and 1. Use place value, known and derived facts to multiply and divide mentally, including: multiplying and
- dividing by a one-digit number Pupils practise to become fluent in the formal written method of short division with exact answers when
- Pupils practise mental methods and extend this to three-digit numbers to derive facts, for example 200 3 = 600 so  $600 \div 3 = 200$
- Pupils solve two-step problems in contexts, choosing the appropriate operation, working with increasingly between 10 children. harder numbers. This should include correspondence questions such as three cakes shared equally



# 5 Divide up to 4 digits by a single digit, including

those with remainders.

Short division, including remainder answers



The answer to 5309 ÷ 8 could be expressed as 663 and five eighths, 663 r 5, as a decimal, or rounded as appropriate to the problem involved.

Short division with remainders: Now that pupils are introduced to examples that give rise to remainder answers, division needs to have a real life problem solving context, where pupils consider the meaning of the remainder and how to express it, ie. as a fraction, a decimal, or as a rounded number or value, depending upon the context of the problem.

See Y6 for how to continue the short division to give a decimal answer for children who are confident.

Calculate.

If children are confident and accurate:

contexts

Include money and measure

Introduce long division for pupils who are ready to divide any number by a 2-digit number (e.g.  $2678 \div 19$ ).

Key Vocabulary: composite number (non-prime) divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, carry', remainder, multiple, divisible by, factor, inverse, quotient, prime number, prime factors share, share equally, one each, two each..., group, equal groups of, lots of, array,

## Key number skills needed for division at Y5:

- Recall multiplication and division facts for all numbers up to  $12 \times 12$  (as in Y4)
- Multiply and divide numbers mentally, drawing upon known facts.
- Identify multiples and factors, including finding all factor pairs of a number, and common factors of two number
- Solve problems involving multiplication and division where larger numbers are decomposed into their factors
- Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000.
- Use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers
- Work out whether a number up to 100 is prime, and recall prime numbers to 19.
- Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context
- Use multiplication and division as inverses
- ing with remainders, as fractions, as decimals or by rounding (e.g.  $98 \div 4 = 24 \text{ r} \ 2 = 24 \text{ /}_2 = 24.5 \approx 25$ ). Interpret non-integer answers to division by expressing results in different ways according to the context, includ-
- Solve problems involving combinations of all four operations, including understanding of the equals sign, and including division for scaling by different fractions and problems involving simple rates.



#### Year 0 Divide at least 4 digits by both single-digit and

2-digit numbers (including decimal numbers and quantities)

Short division, for dividing by a single digit: e.g. 6497 ÷

00 0812125 6497.0000

express the remainder. where pupils have to consider the most appropriate way to life problem solving contexts need to be the starting point, mals, whole number remainders, or rounded numbers. Real understand how to express remainders as fractions, deciuse this method, but with numbers to at least 4 digits, and Short division with remainders: Pupils should continue to

carried onto zeros after the decimal point (to show there was no decimal value in the original number) decimal point is added after the units because there is still a remainder, and the one remainder is Calculating a decimal remainder: In this example, rather than expressing the remainder as r = 1Keep dividing to an appropriate degree of accuracy for the problem being solved

#### Division using chunking:

reducing it gradually until there is either nothing or a remainder left. 'Chunking' is based around repeated subtraction. We take 'chunks' of the number away.

If 10 lots of the divisor

If 10 lots of 16 are 160, 5 lots are 80. I can take 80 away from 116. "How many lots of 16 could we take 2) Here we are left with 116. We know our number isn't big enough to take another 10 lots of 16 away. 3) I have 36 left. I know double 16 is 32 so now I will take 2 lots of 16 4) I have 4 left. There are no more groups of 16 in this number so this is my gway from 16 16 596 916 160 276 36 80 10x 10x ST. X Keep taking 10 lots away until the number is too small to do this 5) Add the total number of groups you took out of 596. There are 37 groups of 16 with 4 left over: 1) Begin by asking: "Can we take 10 lots of 16 away from 596?" 3754

(320) straight away. Some children will go further and recognise instantly that they As the children become more confident, they will start to take larger 'chunks' away from the number. In the example above, we could start by subtracting 20 lots of 16 could begin by subtracting 30 lots of 16 (480).

> cannot be taken away at the first stage, try 9 lots, 8 Division using multiples: lots, 7 lots etc. 24) 854 35 r 14 
>  1x
>  2x
>  3x
>  4x
>  5x
>  6x
>  7x
>
>
>  24
>  48
>  72
>  96
>  120
>  144
>  168
>  multiples of the divisor to help them in their Children write out Calculate, Estimate, Check!

#### Key Vocabulary: As previously, & common factor

## Key number skills needed for division at Y6:

- Recall and use multiplication and division facts for all numbers to  $12 \times 12$  for more complex calculations
- the context. Use short division where appropriate sion, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long divi-
- Perform mental calculations, including with mixed operations and large numbers
- 0 0 Identify common factors, common multiples and prime numbers
- Solve problems involving all 4 operations.
- 0 Use estimation to check answers to calculations and determine accuracy, in the context of a problem.
- Use written division methods in cases where the answer has up to two decimal places.

0

Solve problems which require answers to be rounded to specified degrees of accuracy.